




# 1 Chalkboard: A Library at the Intersection of Pure 2 Mathematics and Web Interactivity

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## Software

- [Review](#) 
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## 5 Summary

6 Chalkboard is a library at the intersection of pure mathematics and web interactivity. It  
7 facilitates the construction and manipulation of computational structures and analytical  
8 systems in JavaScript and Node.js environments.

9 The library provides a comprehensive system of functionalities, including but not limited  
10 to defining isomorphisms between algebraic structures, computing the flux of vector  
11 fields over parameterized surfaces, simulating systems of differential equations, visualizing  
12 statistical regression models, simplifying and evaluating both real- and complex-valued  
13 expressions, executing multidimensional matrix operations, and automating Karnaugh  
14 map minimizations.

15 It enables the creation of exploratory computational lessons, browser-based visualizations,  
16 and self-study materials. Rather than treating mathematics in JavaScript as a thin layer of  
17 numerical utilities, Chalkboard provides explicit mathematical datatypes and operations  
18 that allow pedagogical applications on the web to mirror mathematical structure more  
19 directly.

## 20 Statement of Need

21 Computationally-enabled educational infrastructure for mathematics increasingly takes  
22 place on the web in course websites, interactive demonstrations, and browser-based  
23 notebooks. However, educators and learners who intend to build such resources in raw  
24 JavaScript often face a gap between low-level numerical utilities and the richer mathematical  
25 abstractions needed for formal mathematical exposition.

26 Chalkboard addresses this gap by providing access to structured mathematical objects  
27 and computations in a way that can be integrated into educational materials on the web  
28 just as straightforwardly as one would write educational materials on paper. This lowers  
29 the friction between a mathematical idea and a programmed executable that students can  
30 inspect, manipulate, and learn from directly by opening a web URL, with no additional  
31 setup, installations, or runtime dependencies required.

32 The software may be adopted by others in several ways: instructors can embed Chalkboard-  
33 powered demonstrations into course websites; students can use examples as resources for  
34 autodidactic learning; and authors of educational content can use the library to build  
35 lessons that combine mathematics, programming, and visualization in a single web-oriented  
36 environment.

## 37 Related Work

38 The JavaScript library ecosystem includes many mature mathematical libraries such as  
39 Math.js (Jong & others, 2026), Decimal.js (Mclaughlin, 2025), and stdlib (Reines & others,  
40 2024). These projects are valuable tools for general-purpose computation, but they are  
41 not primarily oriented around establishing accessible, interactive, formal mathematics as a  
42 system of structures.

43 Chalkboard differs from them by emphasizing a comprehensive and coherent API designed  
44 for engagement with mathematics in a web browser that reflects engagement with  
45 mathematics on a paper. Its goal is not to replace specialized computer algebra systems  
46 or high-performance numerical environments, but to support educational workflows in  
47 which mathematical ideas, computation, and visualization are tightly integrated.

## 48 Software Functionality

49 Chalkboard is organized into fifteen topic-oriented namespaces, totaling nearly  
50 seven hundred functions, with a consistent, intuitive call pattern of the form  
51 Chalkboard.namespace.function(parameters);. It also defines a set of eleven custom  
52 datatypes, including objects for complex numbers, matrices, vectors, tensors, quaternions,  
53 morphisms, ordinary differential equations, and algebraic structures.

54 This design is intended to make pedagogical programming more legible by categorizing  
55 operations according to mathematical topic rather than presenting them as an  
56 amalgamation of helper functions. To illustrate this ergonomic approach, consider how  
57 Chalkboard provides a declarative syntax that mirrors the style of writing mathematics  
58 on paper:

```
// Define sets
const Z4 = Chalkboard.abal.Z(4);
const C4 = Chalkboard.abal.C(4);

// Define groups
const G = Chalkboard.abal.group(Z4, (m, n) => (m + n) % 4);
const H = Chalkboard.abal.group(C4, (z, w) => Chalkboard.comp.mul(z, w));

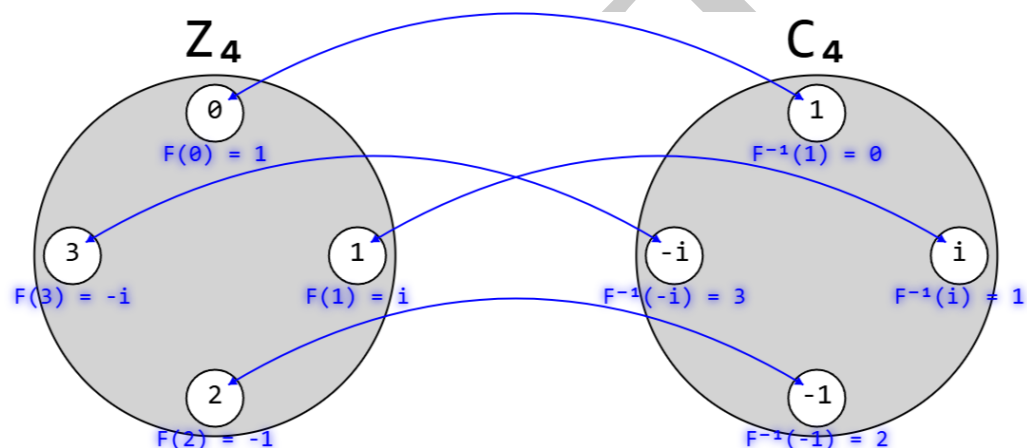
// Define isomorphism
const F = Chalkboard.abal.isomorphism(G, H, (n) => Chalkboard.I(n));
```

59 In the snippet above, Chalkboard defines a group isomorphism  $F : G \rightarrow H$  between  
60 the additive group of integers modulo 4,  $G = (\mathbb{Z}_4, +)$ , and the multiplicative group of  
61 fourth roots of unity,  $H = (\mathbb{C}_4, \times)$ . Rather than treating these as mere arrays, the library  
62 represents them as custom ChalkboardStructure datatypes (recall that it has a total of  
63 eleven custom datatypes, facilitating the functions in various namespaces to be able to  
64 “understand” their mathematical contexts), which allow the Chalkboard.abal namespace  
65 to treat them as virtual algebraic structures, and thus robustly assess the group axioms  
66 for them. This enables the library to verify that the mapping  $F(n) = i^n$  preserves the  
67 underlying structure, or in other words, to verify that the operation in the domain  $G$  is  
68 perfectly mirrored by the operation in the codomain  $H$ .

69 The design of Chalkboard is useful in pedagogical settings because the code can serve  
70 simultaneously as an executable program and as a coherent representation of the  
71 mathematics itself.

## 72 Educational Impact

73 Chalkboard significantly lowers the barrier to entry of creatively and educationally  
74 demonstrating mathematical beauty and curiosity on the web. Its [documentation](#) includes  
75 a variety of [examples](#) to get started with: for physics, Chalkboard can simulate the  
76 [three-body problem](#) with a 12-dimensional ordinary differential equation and model [fluid](#)  
77 [flow](#) using particles moving along a vector field; it supports abstract algebra and number  
78 theory with thorough namespaces that allow visual demonstrations of [group isomorphisms](#)  
79 and [modular arithmetic symmetry](#); it is also highly capable in applied contexts, from  
80 rendering real-time statistical [telemetry dashboards](#) to executing 3D rotations with both  
81 [matrices](#) and [quaternions](#); lastly, it can effectively exhibit classic explanatory graphics,  
82 such as the [Mandelbrot set](#) from complex numbers and [Newton's method](#) from calculus.



The isomorphism  $F: Z_4 \rightarrow C_4$  is defined by  $F(n) = i^n$  for all  $n$  in  $Z_4$ .

The inverse isomorphism  $F^{-1}: C_4 \rightarrow Z_4$  is defined by  $F^{-1}(z) = (2/\pi) \cdot \arg(z) \bmod 4$  for all  $z$  in  $C_4$ .

**Figure 1:** Chalkboard is used to visualize the group isomorphism between the integers modulo 4 ( $Z_4$ ) and the fourth roots of unity ( $C_4$ ).

83 A recent addition is an experiment-oriented example which is an [ODE solver error vs step](#)  
84 [size study](#) that compares multiple fixed-step ODE solvers across step counts, computes  
85 error metrics, estimates observed convergence order, generates plots, and exports results  
86 in machine-readable CSV/JSON formats. Therefore, Chalkboard can support not only  
87 visual demonstrations but also computational lessons in numerical analysis.

88 At present, Chalkboard has primarily been used to create self-contained interactive  
89 demonstrations rather than as a part of a formally deployed classroom platform. However,  
90 the software is explicitly designed for straightforward adoption because it runs natively in  
91 standard web environments without having any heavyweight runtime requirements.

## 92 Availability

93 Chalkboard is free and open-source at its [repository on GitHub](#) under the [Mozilla Public](#)  
94 [License 2.0](#).

## 95 Acknowledgements

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100 source implementation (JentGent, 2023) of QR decomposition that was adapted into the  
101 matrix namespace.

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